## Elementary Statistics

## Study Guide 20

Due Date: $\qquad$

Name: $\qquad$
Class: $\qquad$
Score: $\qquad$

Your work must be very similar to my notes, lectures, or videos.
Be Neat, Organized, and No Work $\Leftrightarrow$ No Points

1. Consider the data $2,4,6,8,10,12$, and 14. Store them in $L_{1}$, and then
(a) (2 points) find $\mu$.
(a) $\qquad$
(b) (2 points) find $\sigma$.
(b)
(c) (3 points) find $\sigma^{2}$.
(c)
(d) (2 points) Take samples of size 2 with replacement from this population, list all your samples in the table below:

| 2,2 | 2,4 | 2,6 | 2,8 | 2,10 | 2,12 |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
| 4,2 | 4,4 |  |  |  |  |  |
| 6,2 |  |  |  |  |  |  |
| 8,2 |  |  |  |  |  |  |
| 10,2 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |

(e) (2 points) Now find the mean of each sample, and place all the sample means in the table below:

| 2 | 3 | 4 | 5 | 6 | 7 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3 | 4 |  |  |  |  |  |
| 4 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |

(f) (3 points) Complete the following probability distribution table for all the sample means: Write $P(\bar{x})$, in fractions( do not reduce).

| $\bar{x}$ | $P(\bar{x})$ | $\bar{x}$ | $P(\bar{x})$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $\frac{0}{49}$ |  |  |
| $\mathbf{2}$ | $\frac{1}{49}$ |  |  |
| $\mathbf{3}$ | $\frac{2}{49}$ |  |  |
| $\mathbf{4}$ |  |  |  |
|  |  |  |  |
|  |  |  |  |

(g) (6 points) Draw the probability distribution histogram using $\bar{x}$ and $p(\bar{x})$ superimposed with a bell curve. Clearly label and mark your graph.


Now enter all the sample means $\bar{x}$ in $L_{2}$, and corresponding probabilities $P(\bar{x})$ in $L_{3}$.
(h) (2 points) find $\mu_{\bar{x}}$.
(h) $\qquad$
(i) (2 points) find $\sigma_{\bar{x}}$.
(i) $\qquad$
(j) (3 points) find $\sigma_{\bar{x}}^{2}$.
(j) $\qquad$
2. With a sample size $n=16$ of the normally distributed population with the mean of $\mu=6500$ and standard deviation of $\sigma=275$,
(a) (2 points) find $\mu_{\bar{x}}$.
(a)
(b) (3 points) find $\sigma_{\bar{x}}$.
(b)
3. With a sample size $n=25$ of the normally distributed population with the mean of $\mu=125$ and standard deviation of $\sigma=10$,
(a) (2 points) find $\mu_{\bar{x}}$.
(a) $\qquad$
(b) (3 points) find $\sigma_{\bar{x}}$.
(b)
4. The heights of a certain breed of dogs has a normal distribution with a mean of 28 inches and a standard deviation of 4 inches. If we randomly select 64 of these dogs, what is probability that the mean height of 64 dogs is
(a) (3 points) less than 27 inches?
(a)
(b) ( $\mathbf{3}$ points) greater than 28.5 inches?
(b)
5. The average life of a certain blender is 4.5 years with a standard deviation of 1.25 years. Assuming that the lives of these blenders follow approximately a normal distribution, find
(a) (3 points) the probability that the mean life of a random sample of 8 such blenders fall between 4 and 6 years.
(a)
(b) (4 points) the value of $\bar{x}$ that separates the top $15 \%$ from the rest for a random sample of 8 such blenders. Round your answer to one decimal place.
(b)

